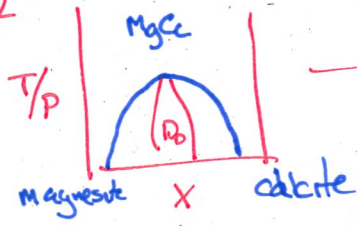


10 [12] possible problemsets $\Rightarrow$ 9 count
 0, 1, 2, 4, 4b, 5, 6, 8a, 8b, 11, [9.1], [7]

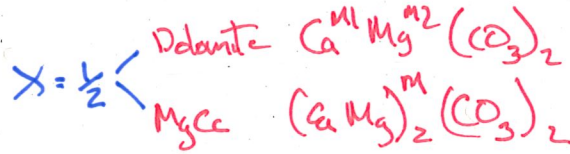
Problem 0.1 $\rightarrow$ solvus $\rightarrow$ Chp 8.1 (solvus can be calculated quantitatively w/ script for problem 9.1)
 Problem 0.3, 0.4 $\rightarrow$ Chp 6 (9)
 Problem 0.2

Chapter 11.1 2022

$\downarrow$
 Note correction (yesterday)
 to Eq 11.11 $g = g' / \sqrt{z}$



ergodic hypothesis does not allow variable order



Why?

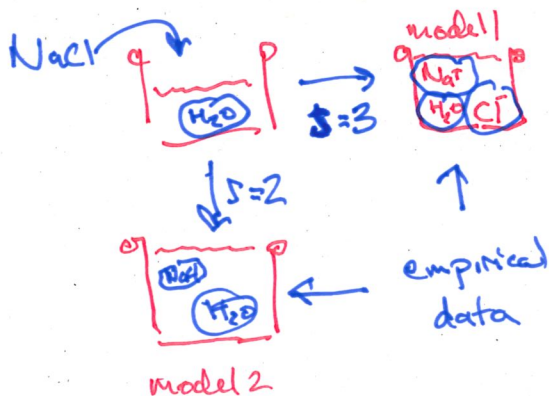
	S_{conf}	S_{sub}	$\rightarrow$ measured by G_p usually referred to as "enthalpic stabilization"
Do	Low	high	
MgCc	high	low	

Speciation (aka order-disorder or compound formation) models. Components vs. Species

Water $\rightarrow C = 1 \rightarrow \text{H}_2\text{O}$, max $C = 2 \rightarrow \text{H}_2, \text{O}_2 \rightarrow C \leq \#$ of elements
 if stoichiometric | if nonstoichiometric

physics $\rightarrow$ t -species $\text{H}_2\text{O}, \text{H}_2, \text{O}_2, \text{OH}, \text{H}^+, \text{H}_2\text{O}_2, \dots$ there is no thermodynamic restriction on species $\rightarrow$ used in thermo only to facilitate (simplify) empirical solution models

Two kinds of speciation models $\rightarrow$ Primitive $\rightarrow t=c$ endmembers
 $\rightarrow$ microscopic speciation stoichiometrically prescribed (ergodic)
 $\rightarrow$ nothing new (plagioclase) $\rightarrow$ looks different for fluids and melts: $\text{NaCl} + \text{H}_2\text{O} \Rightarrow C=2 (!)$



$y \rightarrow$ endmember fraction ($\sum = 1$)

$z \rightarrow$ species fraction ($\sum = 1$)

$n_{\text{tot}} \rightarrow$ total number of moles of species

$$n_{\text{tot}} = y_{\text{H}_2\text{O}} + z y_{\text{NaCl}} \Rightarrow y_{\text{H}_2\text{O}} = 1 - y_{\text{NaCl}} = 1 + y_{\text{NaCl}}$$

$$S=3 \text{ cont'd} \Rightarrow z_{\text{Na}^+}^* = \frac{n_{\text{Na}^+}}{n_{\text{TOT}}} = \frac{y_{\text{NaCl}}}{1+y_{\text{NaCl}}} [= z_{\text{Cl}^-}]$$

$$z_{\text{H}_2\text{O}} = \frac{n_{\text{H}_2\text{O}}}{n_{\text{TOT}}} = \frac{1-y_{\text{NaCl}}}{1+y_{\text{NaCl}}}$$

$$\begin{aligned} -\frac{S^{\text{conf}}}{R} &= z_{\text{Na}^+} \ln z_{\text{Na}^+} + z_{\text{Cl}^-} \ln z_{\text{Cl}^-} + z_{\text{H}_2\text{O}} \ln z_{\text{H}_2\text{O}} \\ &= 2 \frac{y_{\text{NaCl}}}{1+y_{\text{NaCl}}} \ln \left(\frac{y_{\text{NaCl}}}{1+y_{\text{NaCl}}} \right) + \frac{1-y_{\text{NaCl}}}{1+y_{\text{NaCl}}} \ln \left(\frac{1-y_{\text{NaCl}}}{1+y_{\text{NaCl}}} \right) \end{aligned}$$

$\swarrow$ y_{NaCl} $\swarrow$ y_{NaCl} $\swarrow$ $y_{\text{NaCl}} \rightarrow 0$

$$-\frac{S^{\text{conf}}}{R} = y_{\text{NaCl}} \ln y_{\text{NaCl}}^2 = y_{\text{NaCl}} \ln (a_{\text{NaCl}}^{\text{ideal}}) \quad a_{\text{NaCl}}^{\text{ideal}} = y_{\text{NaCl}}^2$$

Intro chemistry

model 2 $S=2$

$$\begin{aligned} -\frac{S^{\text{conf}}}{R} &= y_{\text{NaCl}} \ln y_{\text{NaCl}} + y_{\text{H}_2\text{O}} \ln y_{\text{H}_2\text{O}} \quad y_{\text{NaCl}} \rightarrow 0 \\ &= y_{\text{NaCl}} \ln a_{\text{NaCl}} \quad a_{\text{NaCl}} = y_{\text{NaCl}} \end{aligned}$$

silicate melt models are generally of this form ($t=c$)

Non-ergodic speciation models (order-disorder, compound formation)

$\Rightarrow t > c$ endmembers (species)

$\Rightarrow t = c$ speciation reactions

eg $\text{H}_2\text{O} \Rightarrow c=2 \quad t = \{\text{H}_2, \text{O}_2, \text{H}_2\text{O}\} = 3$ speciation reaction
 $\text{H}_2 + \frac{1}{2} \text{O}_2 = \text{H}_2\text{O}$
 $\Delta G^\circ \neq 0$

$c=1 \Rightarrow$ solution model $\Rightarrow$ oxygen $O [O_2, O_3, \dots]$ & Thermodynamics

$t=2 \Rightarrow O_2, O_3$ species $\leftarrow$ physics

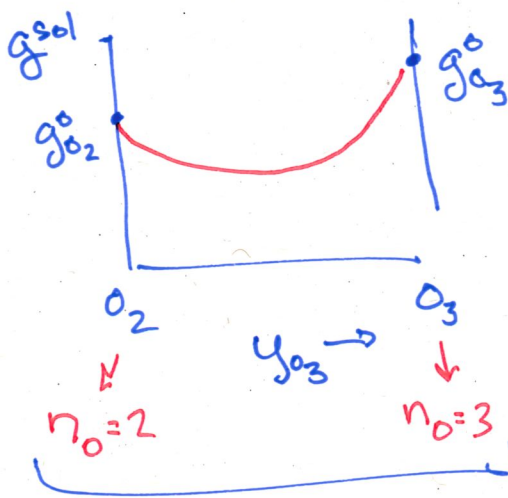
$t-c=1 \Rightarrow$ speciation reaction, $\frac{3}{2}O_2 - \frac{2}{3}O_3 = 0 \quad \Delta\alpha = 3-2=1$

$$g^{sol} = \sum_{i=1}^t y_i g_i^0 - T s_{cont} + g^{ex} \rightarrow \text{for simplicity}$$

for ~~homogeneous~~ internal phase relations c of the g_i^0 values may be set $=0 \Rightarrow \sum_{i=1}^t y_i \Delta g_i^0 = y_{O_3} \Delta g_{O_3}^0$

$$g^{sol} = \sum y_{O_3} \Delta g_{O_3}^0 - RT (y_{O_3} \ln y_{O_3} + y_{O_2} \ln y_{O_2})$$

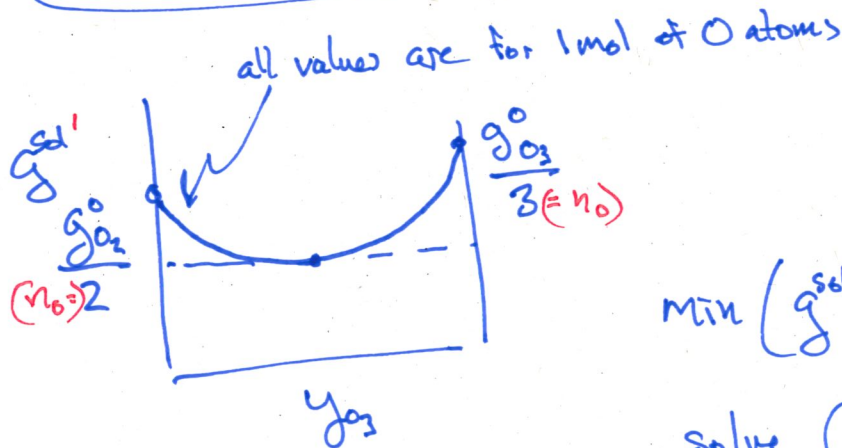
$\Rightarrow$ eliminate $y_{O_2} (=1-y_{O_3}) \Rightarrow g(y_{O_3})$



$g^{sol} \rightarrow$ is $g/\text{mole-of-species}$
we need $g/\text{mole-of-atoms}$
~~For an initial~~ $n_O = 2 + y_{O_3}$

$$g^{sol'} = g^{sol} / n_O = g^{sol} / (2 + y_{O_3})$$

$\hookrightarrow$ generalization in Chp 11 eqs 6-11



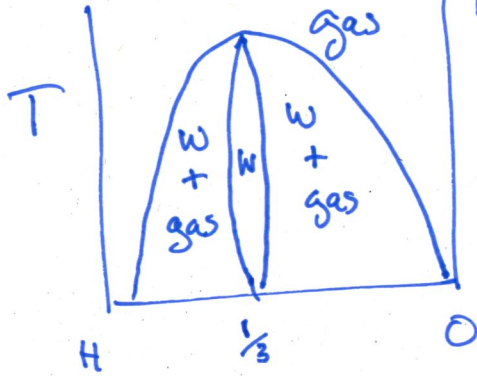
$$\min(g^{sol'}(y_{O_3})) \Rightarrow$$

$$\text{solve } (d.f.f(g^{sol'}, y_{O_3}))$$

$$C > 2 \quad t > C$$

convergent ordering

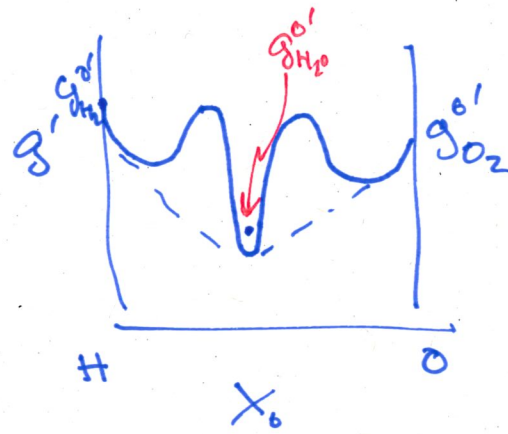
H-G, $C=2$



$P < P_{crit} \sim 21 \text{ bar}$

$$C=2$$

$$t=3 = \left\{ \begin{matrix} \text{H}_2 \\ \text{O}_2 \\ \text{H}_2\text{O} \end{matrix} \right\}$$



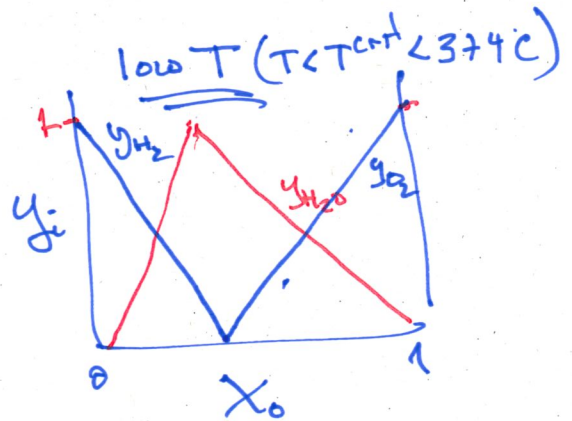
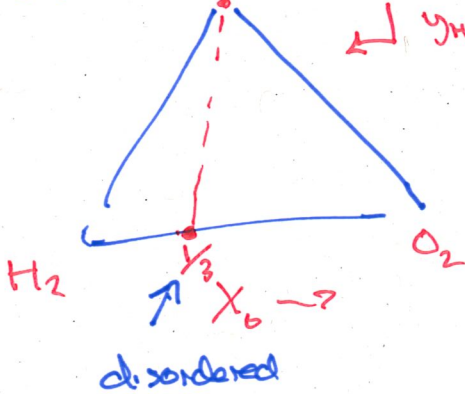
$$X_0 \rightarrow$$

$$\downarrow$$

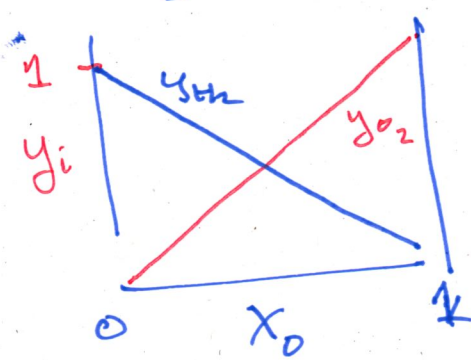
Bulk composition

ordered $\rightarrow$ H_2O Speciation composition

$$\leftarrow y_{\text{H}_2\text{O}}, y_{\text{H}_2}, y_{\text{O}_2}$$



high $T \Rightarrow y_{\text{H}_2\text{O}} = 0$



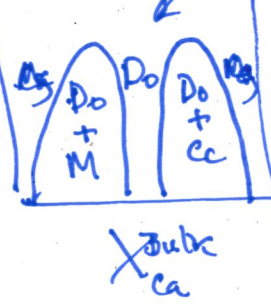
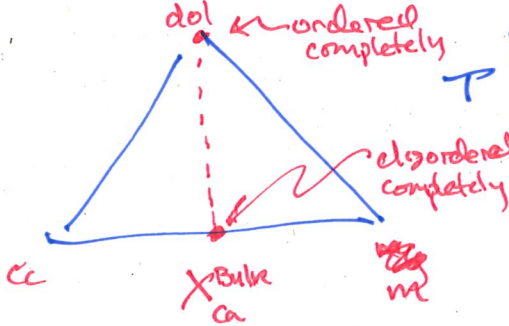
solids do-cc-m (problem 11.1 omphacite jd-di-cm)

$$C=2 \quad \{ \text{CaCO}_3, \text{MgCO}_3 \}$$

means there MUST be 2 crystallographically distinct sites for Ca/Mg

$$t=3 \quad \{ \text{CaCO}_3, \text{MgCO}_3, \text{Ca}_{0.5}\text{Mg}_{0.5}\text{CO}_3 \}$$

non-convergent (no transition to completely disordered phase)



$\Rightarrow$ we need $y_{\text{sol}}(X_{\text{Ca}}, y_{\text{dol}})$

Endmember site occupancies
and multiplicities

	M1	M2
cc	Ca	Ca
m	Mg	Mg
do	Mg	Ca
$\frac{g_i}{b}$	$\frac{1}{2}$	$\frac{1}{2}$

1) Formulate $g^{sol}(y)$

$$g^{mech} = y_{cc} g_{cc}^0 + y_m g_m^0 + y_{do} g_{do}^0 \Rightarrow c=2 \rightarrow s=0$$

For internal phase relations we may set $g_{cc}^0 = g_m^0 = 0$

$$\text{and } g^{mech} = y_{do} g_{do}^0 \quad (g_{do}^0 = \Delta g^0 \text{ for the pure ordering rxn})$$

$$g^{conf} = -RT \left\{ \frac{1}{2} \left[z_{Ca}^{M1} \ln z_{Ca}^{M1} + z_{Mg}^{M1} \ln z_{Mg}^{M1} \right] + \frac{1}{2} \left[z_{Ca}^{M2} \ln z_{Ca}^{M2} + z_{Mg}^{M2} \ln z_{Mg}^{M2} \right] \right\}$$

$$\text{From site occupancy table } z_{Ca}^{M1} = y_{cc} \quad z_{Mg}^{M1} = 1 - y_{cc}$$

$$z_{Mg}^{M2} = y_m \quad z_{Ca}^{M2} = 1 - y_m$$

$g^{ex} = 0$ for simplicity, in general an excess function
as in normal solutions (and in problem 11.1)

2) convert to $g^{sol}(X_{Ca}, y_{do})$

$$a) \quad X_{Ca} = \frac{n_{Ca}}{n_{Ca} + n_{Mg}}$$

$$n_{Ca} = y_{cc} + \frac{1}{2} y_{do}$$

$$n_{Mg} = y_m + \frac{1}{2} y_{do}$$

$$n_{tot} = y_{cc} + y_m + y_{do} = 1$$

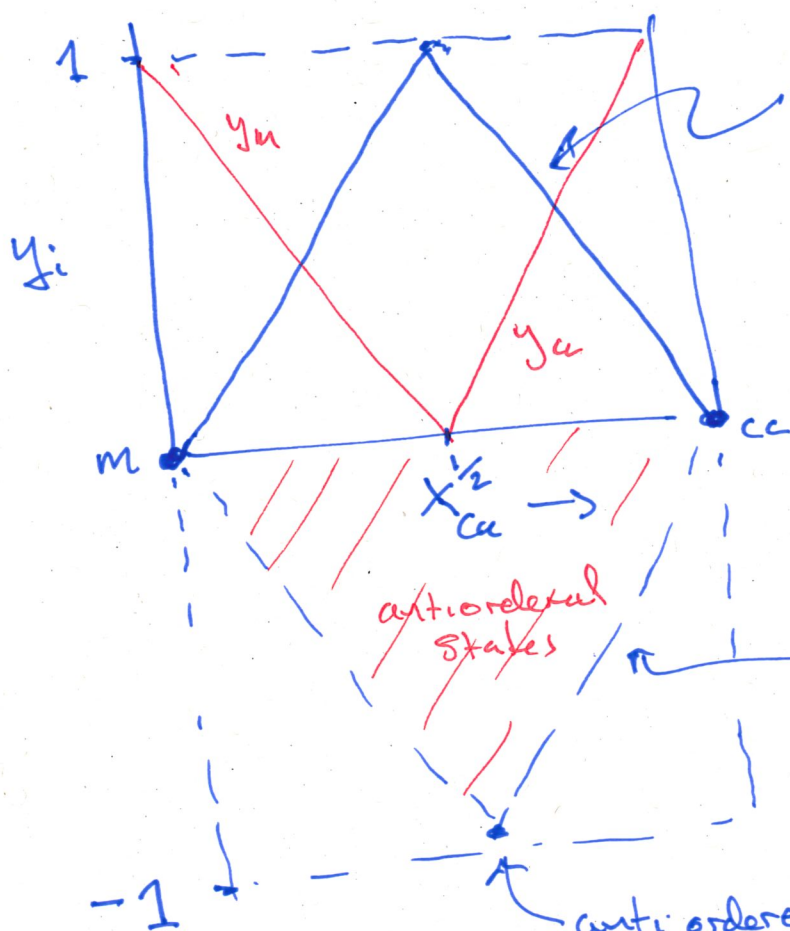
$$X_{Ca} = y_{cc} + \frac{1}{2} y_{do}$$

$$g(X_{Ca}, y_{do}, y_m) \Leftrightarrow y_{cc} = X_{Ca} - \frac{1}{2} y_{do}$$

b) use closure to eliminate $y_m \Rightarrow$

$$y_m = 1 - y_{cc} - y_{do} \Rightarrow y_{cc} = x_{ca} - \frac{1}{2} y_{do}$$

$$y_m = 1 - x_{ca} - \frac{1}{2} y_{do} \Rightarrow g(x_{ca}, y_{do})$$



$\max(y_{do})$ - fully ordered
ignoring antiordered states

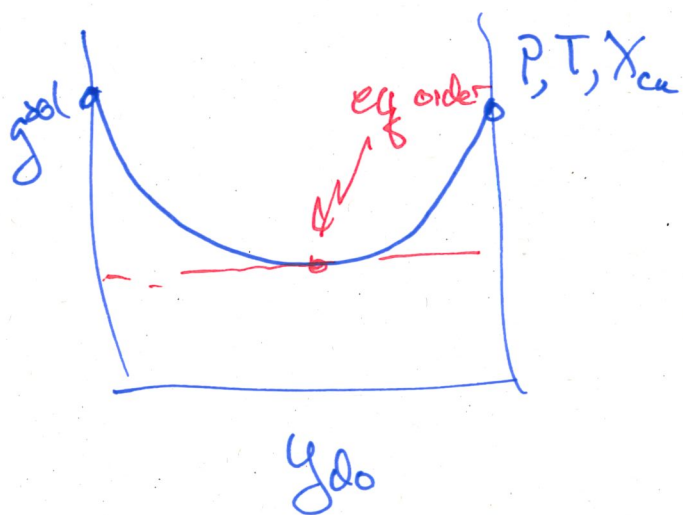
if $x_{ca} < \frac{1}{2}$

$$y_{do, \max} = 2x_{ca}$$

if $x_{ca} > \frac{1}{2}$

$$y_{do, \max} = 2(1 - x_{ca})$$

antiordered (true min y_{do})
($y_{do, \min} = -y_{do, \max}$)



$\min(g^{\text{sol}})$ at cst P, T, x_{ca}

$\Rightarrow$

solve ($\text{diff}(g, y_{do} = 0 \dots y_{do, \max})$)

and x_{ca} or $y_{do, \min}$

given y_{do} ; y_{cc} and y_m
can be obtained by back
substitution

Order parameters

$$Q = [-1, 1]$$



usually expressed as the difference in site fractions for some element, eg here (and in problem 11.1)

$$Q = z_{Mg}^{M1} - z_{Mg}^{M2} = (y_{M1} + y_{do}) - (y_{M1}) = y_{do}$$

Why bother?
