



Stability (Chapter 3)

why wasn't stability an issue in the Al_2SiO_5 phase diagram?

Reversible processes $\Rightarrow dU = \dots \Rightarrow$ external influence required!!
 Spontaneous process $\Rightarrow dS^{universe} > 0 \Rightarrow$ possible w/o external influence.

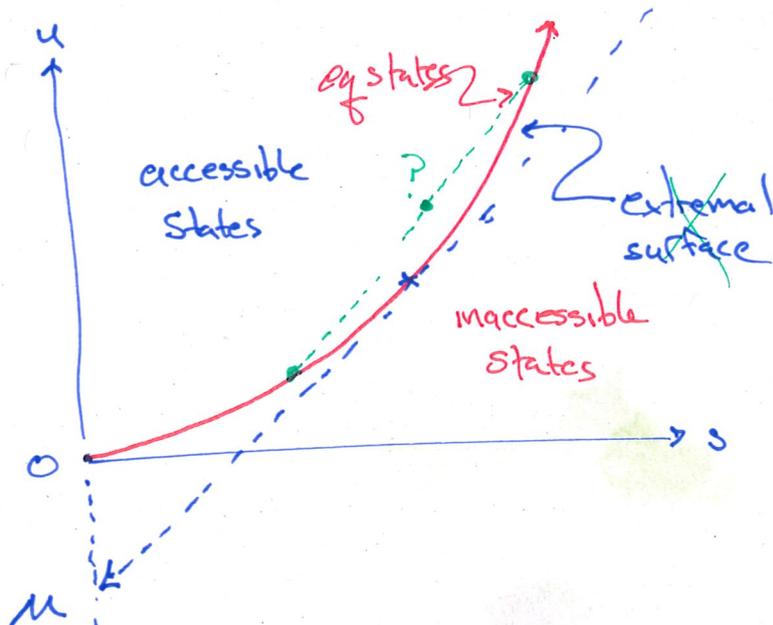
Isolated system \Rightarrow no external influence possible, $dQ = dW = 0, dS > 0$
 a simplified universe with no mechanics:

$$U = TS + \mu N \Rightarrow d = N$$

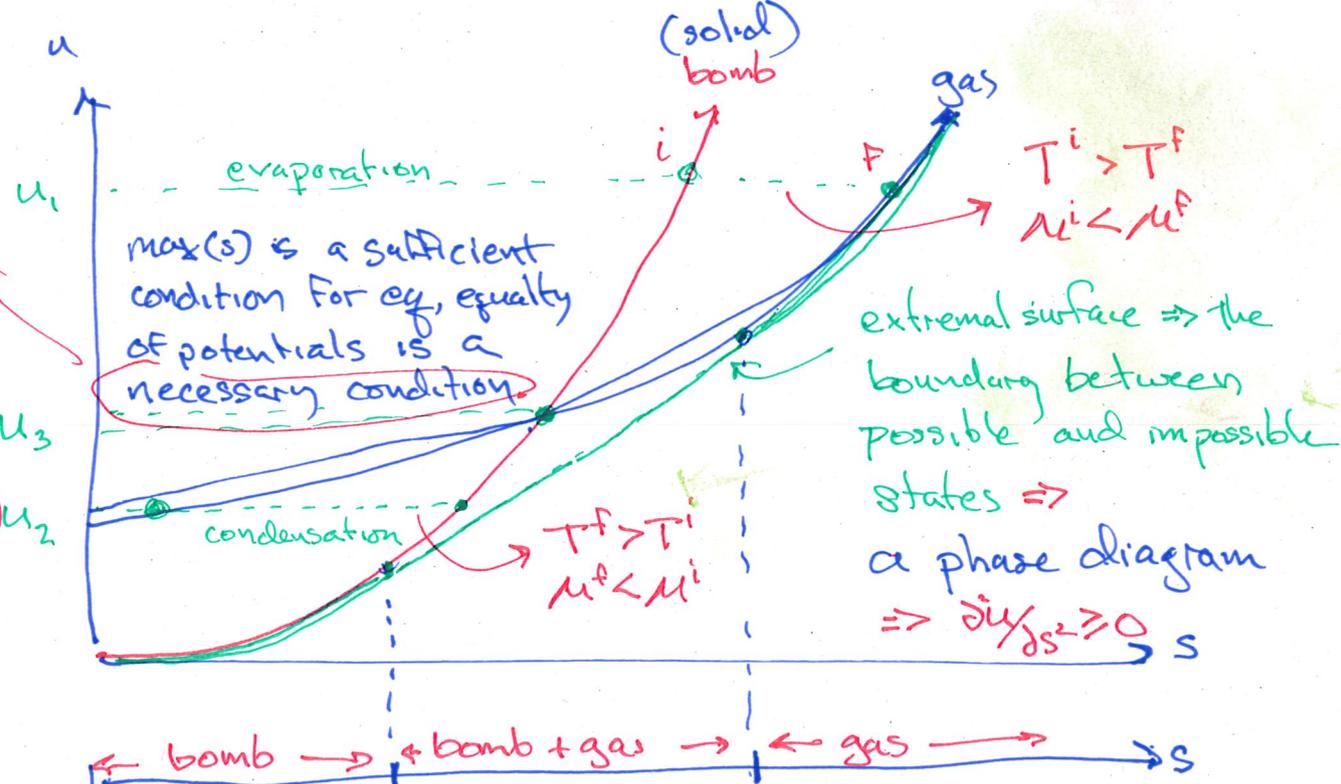
$$u = Ts + \mu \rightarrow dz = 1$$

$$du = Tds$$

$$p = ?$$



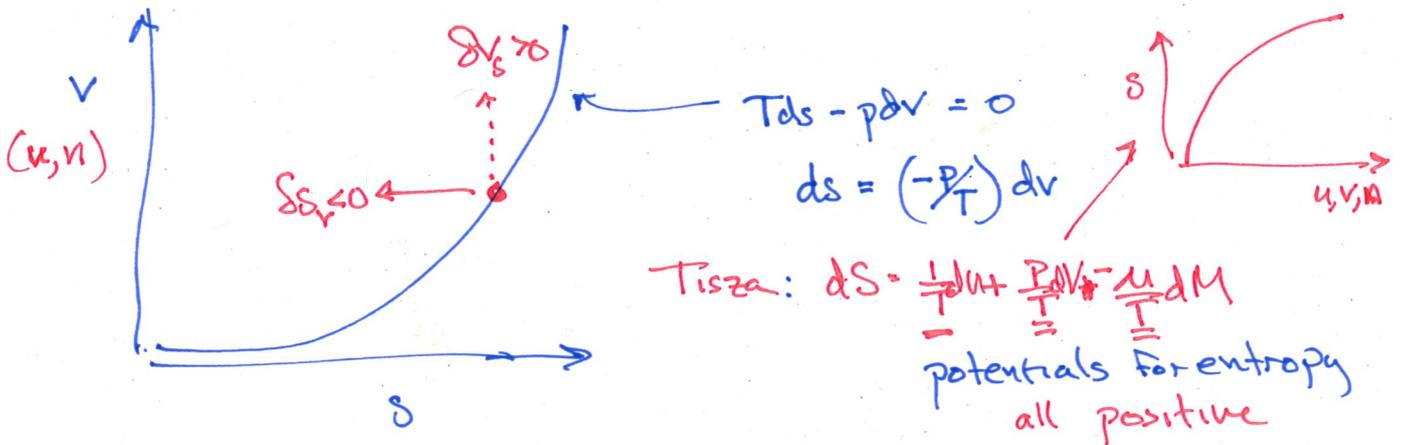
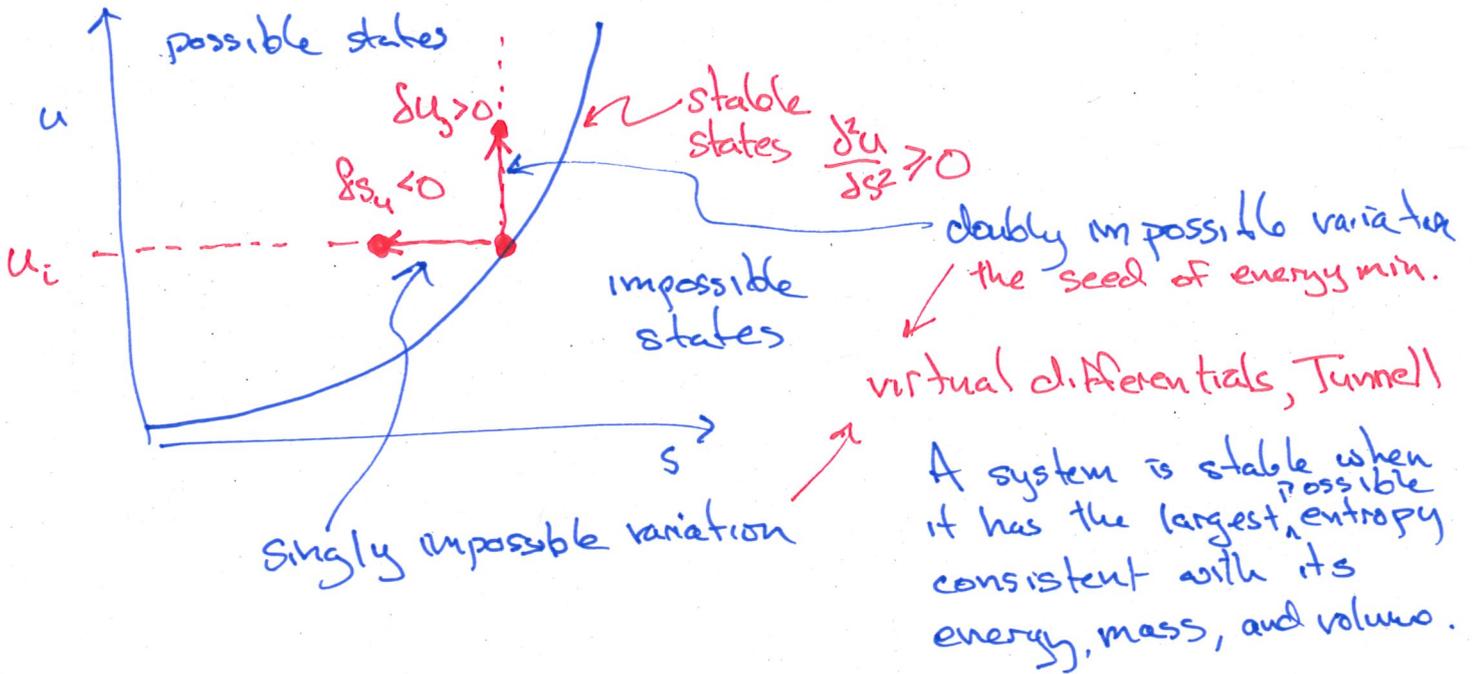
aka "Kuhn-Tucker" conditions + noise + something else. (Karush!)



$$\frac{\partial^2 u}{\partial s^2} = \frac{\partial}{\partial s} \left(\frac{\partial u}{\partial s} \right) = \frac{\partial T}{\partial s} \geq 0$$

$$\frac{\partial^2 u}{\partial s^2} = 0 \text{ when } p = p_{max} \text{ (here } k+1=2)$$

A family of irrational stability criteria



$du = -pdv \Rightarrow$ if u is a minimum

$\frac{\partial u}{\partial v} > 0 \Rightarrow \frac{\partial^2 u}{\partial v^2} = \frac{\partial}{\partial v} \frac{\partial u}{\partial v} = \frac{\partial(-p)}{\partial v} > 0$

$\frac{\partial u}{\partial n} > 0 \Rightarrow \frac{\partial^2 u}{\partial n^2} = \frac{\partial}{\partial n} \left(\frac{\partial u}{\partial n}\right) = \frac{\partial \mu}{\partial n} > 0$

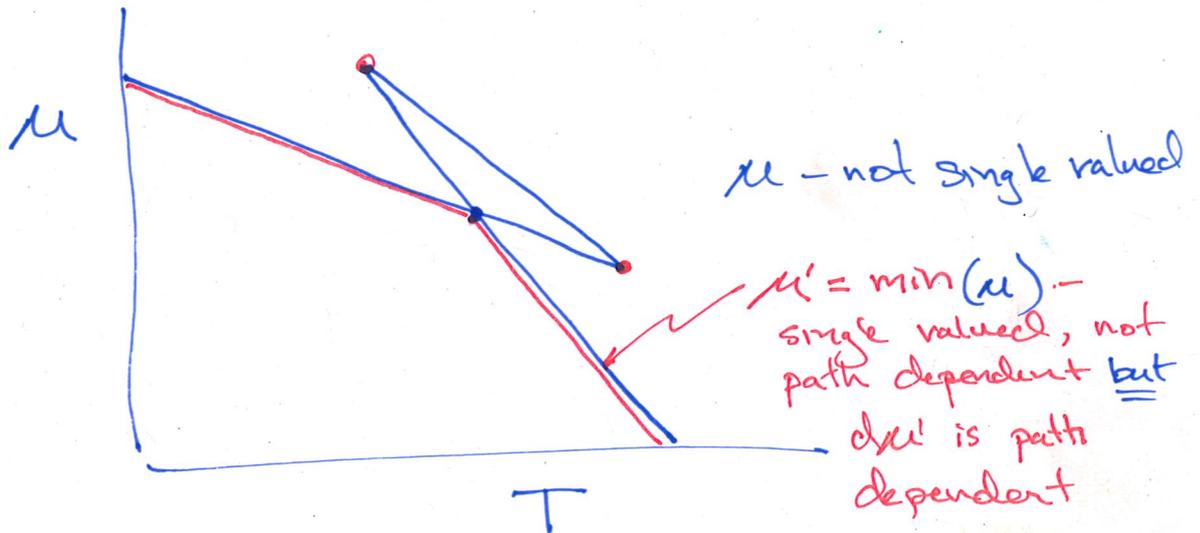
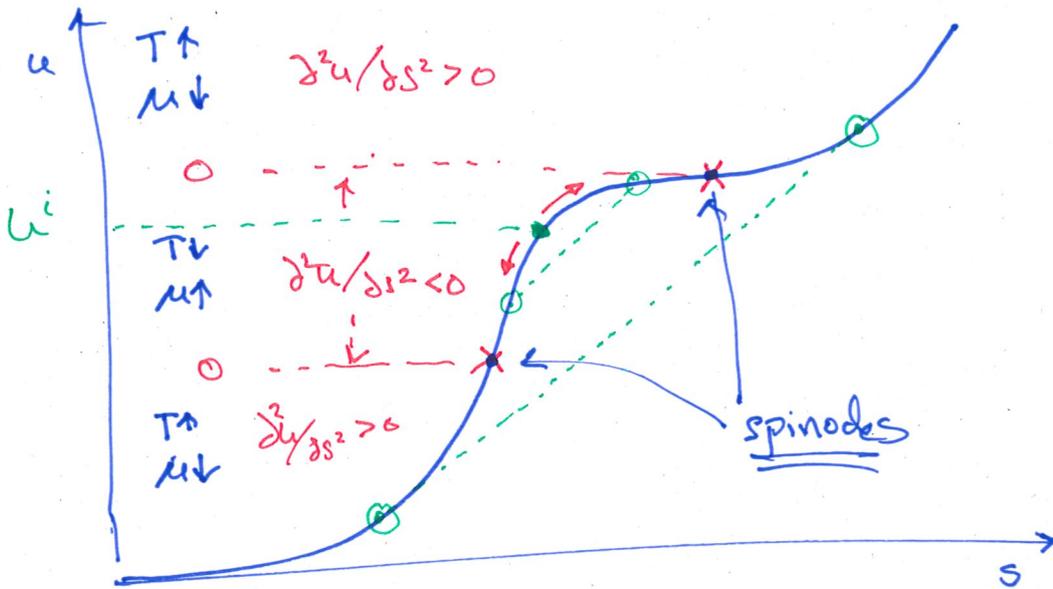
if $s(v, u, n)$ is convex $\frac{\partial^2 s}{\partial v^2} < 0$

then $u(s, v, n)$ $\frac{\partial^2 u}{\partial v^2} > 0$

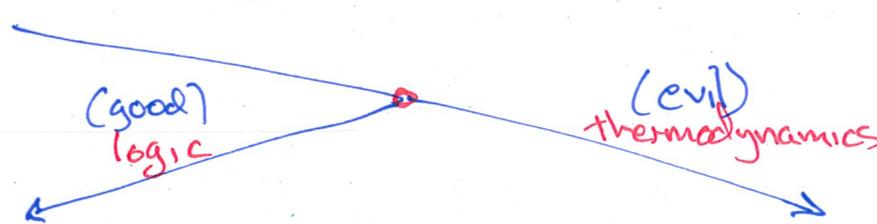
$v(s, u, n)$ \uparrow

$n(s, u, v)$ must be concave

why can't $\partial^2 u / \partial s^2$ be < 0 ?



Stability criterion: a system is stable when NO processes are possible



if there is a state such that $\delta S_{u,v,m} > 0$ then a process is possible.

$\delta S_{u,v,m} > 0$ is a criterion for possible processes [Clausius]

A system is stable when any variation [by definition an impossible variation] to a possible state at cst u, v, m decreases entropy, i.e. $\delta S_{u,v,m} < 0$